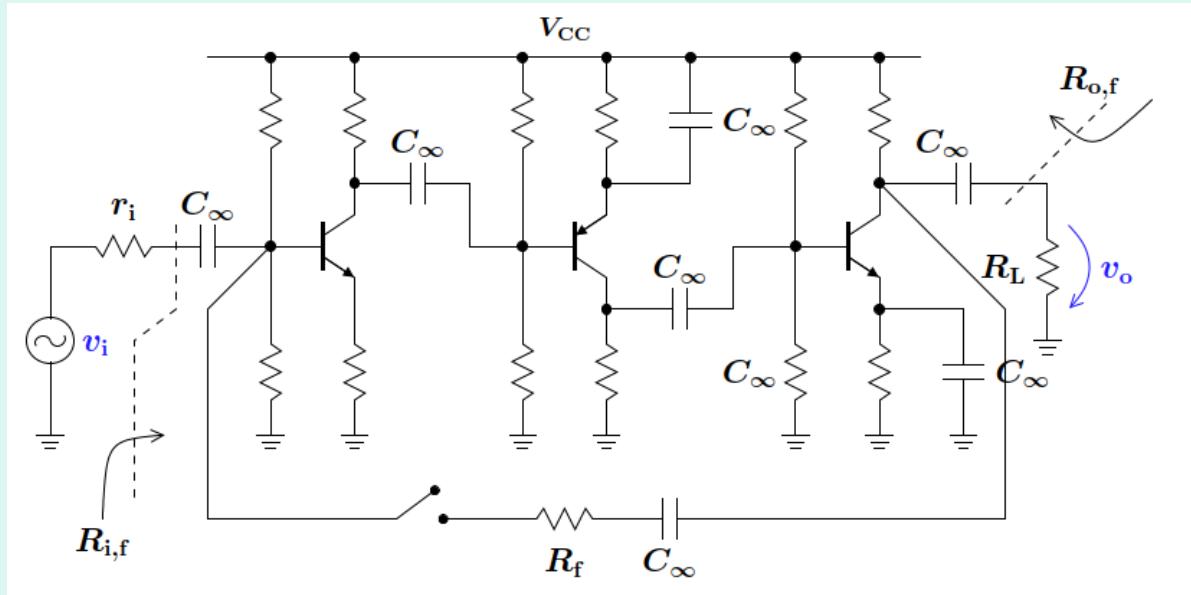
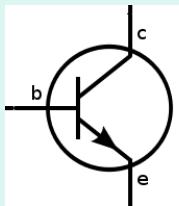


ELEC 301 - CB amplifier configuration

L14 - Oct 07

Instructor: Edmond Cretu

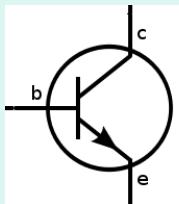




Last lecture

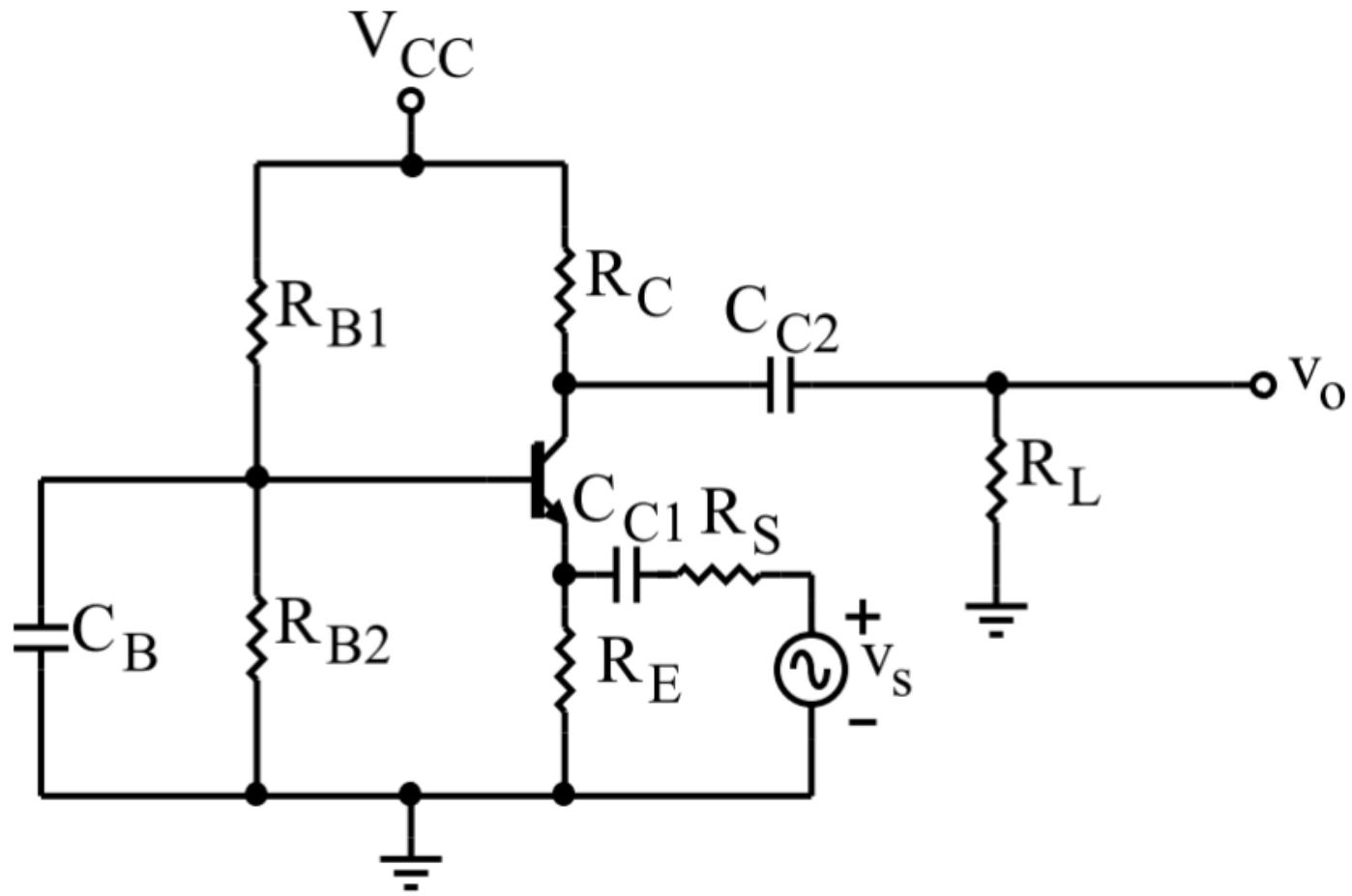
- Analysis of common-emitter configuration - from biasing to AC small signal analysis
- Complex transfer function - 5 poles, 3 zeros - difficult to analyze without fast and approximate analysis methods
- Lessons:
 - HF response limited by internal capacitors (C_μ magnified by the Miller effect)
 - Mid-band - voltage amplification
 - LF response limited by the coupling capacitors - because the “demagnification” of the resistance in the B when seen from E, C_E usually gives ω_{L3dB}

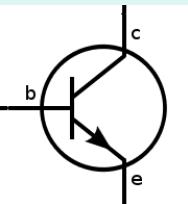




The common-Base amplifier

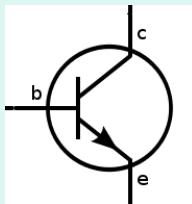
- Input port: E, Output port: C
- We assume proper biasing (1/3 rule); C_B to ground B in AC mode





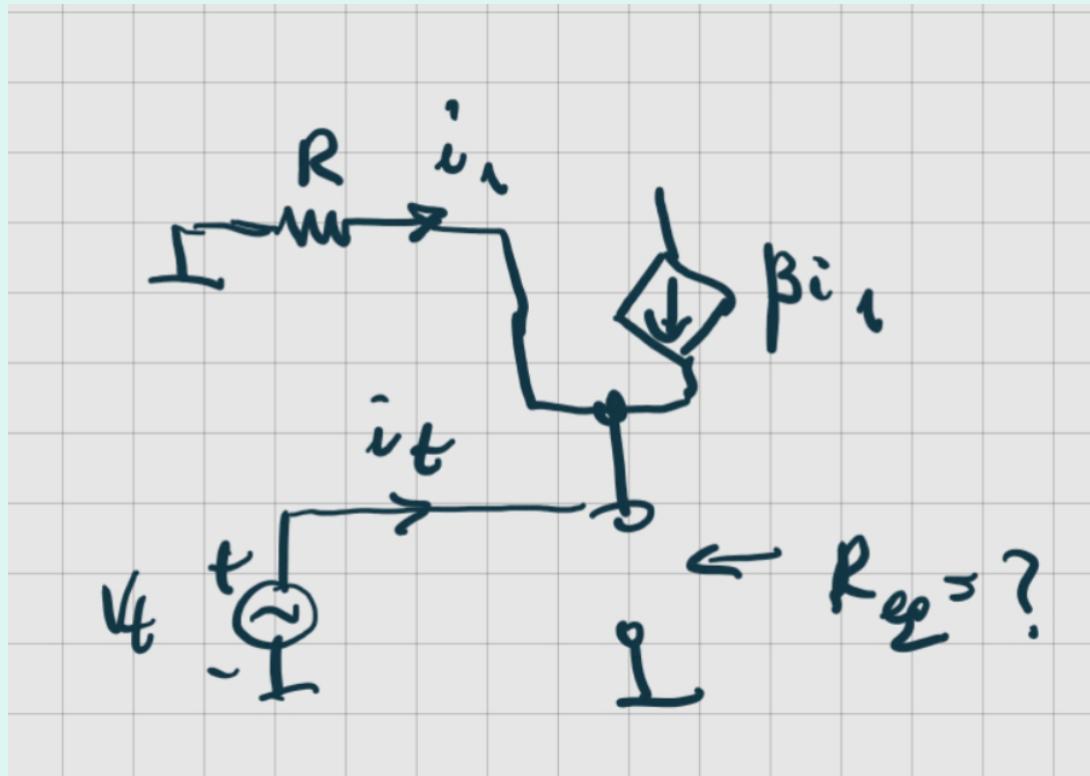
L14 Q01 - ideal voltage amplifier

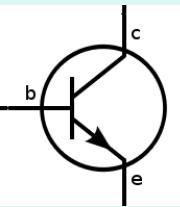
- What are the input and output impedances of an ideal voltage amplifier diport?
 - A. $Z_{in}=0, Z_{out}=\infty$
 - B. $Z_{in}=\infty, Z_{out}=0$
 - C. $Z_{in}=0, Z_{out}=0$
 - D. $Z_{in}=\infty, Z_{out}=\infty$



L14 Q02 - equivalent impedance

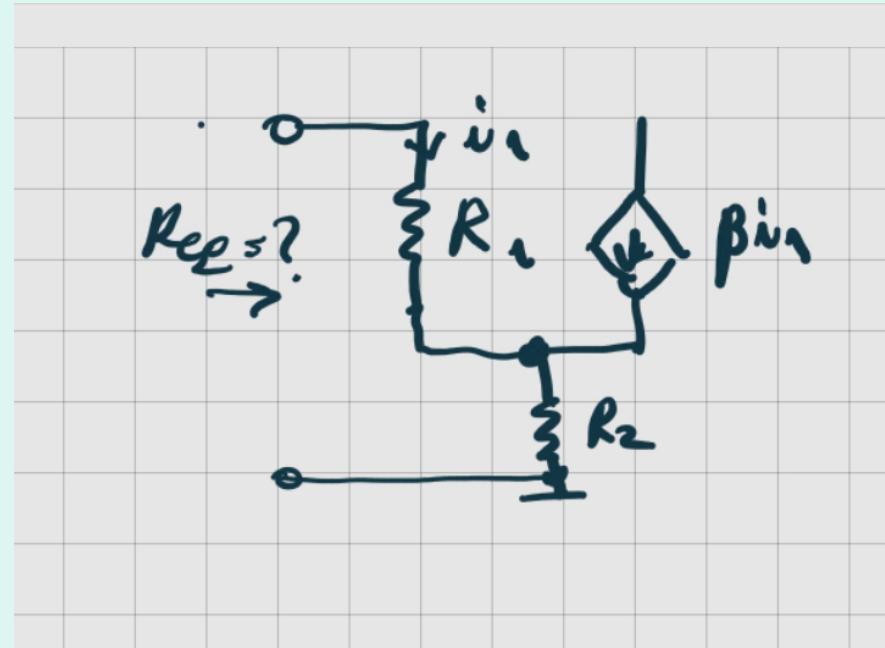
- What is the equivalent input resistance?
 - A. $R(1+\beta)$
 - B. $R/(1+\beta)$
 - C. R
 - D. $R/(1-\beta)$

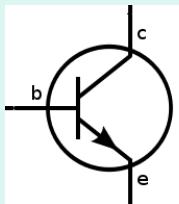




L14 Q03 - equivalent impedance (2)

- What is the equivalent input resistance?
 - A. $R_1 + R_2$
 - B. $R_1 + R_2 / (\beta + 1)$
 - C. $(\beta + 1)R_1 + R_2$
 - D. $R_1 + (\beta + 1)R_2$

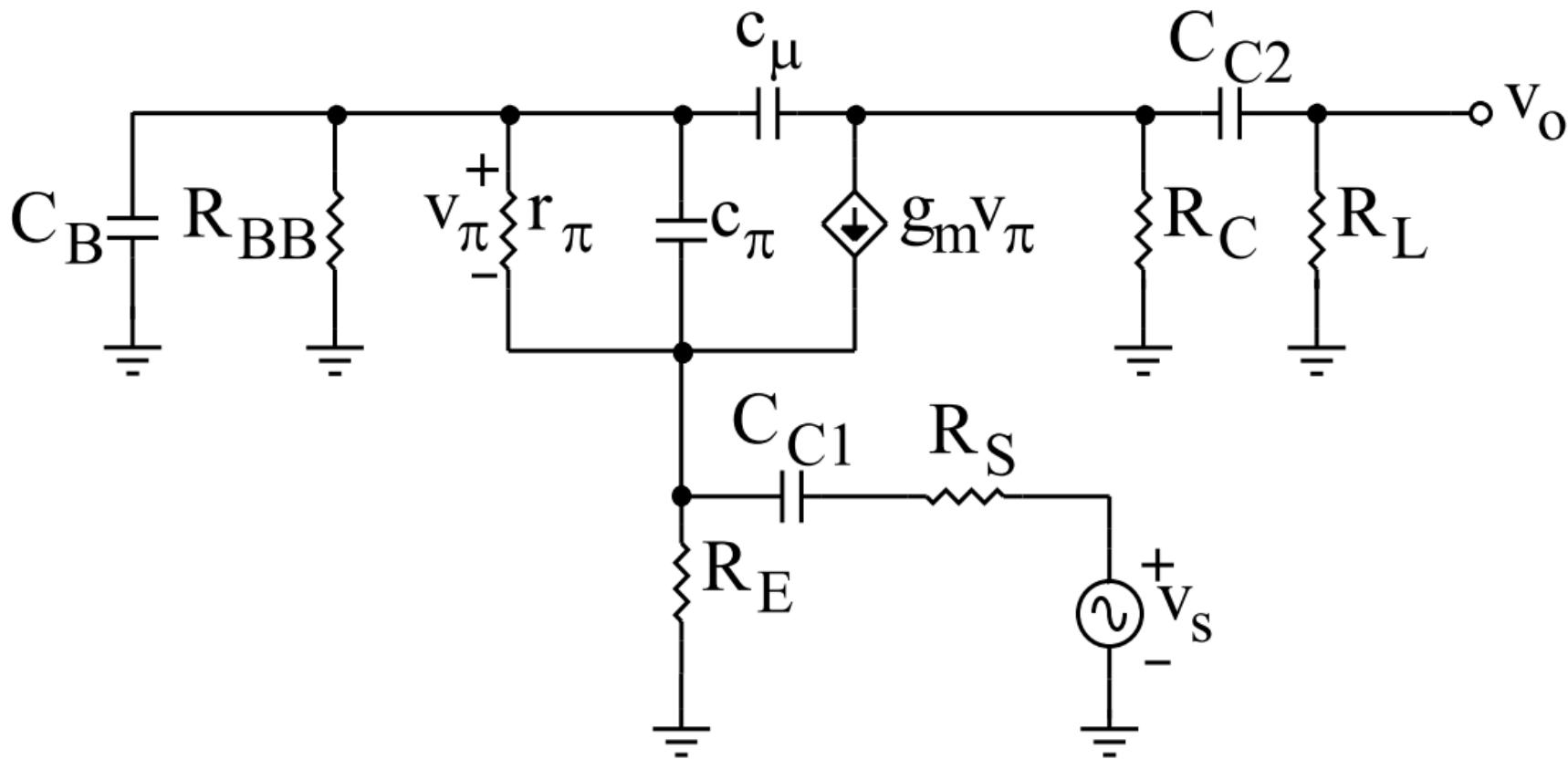


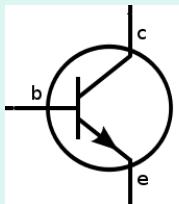


Small-signal model

- Start with small signal circuit
- C_B, C_{C1}, C_{C2} - LF capacitors
- C_μ, C_π - HF capacitors

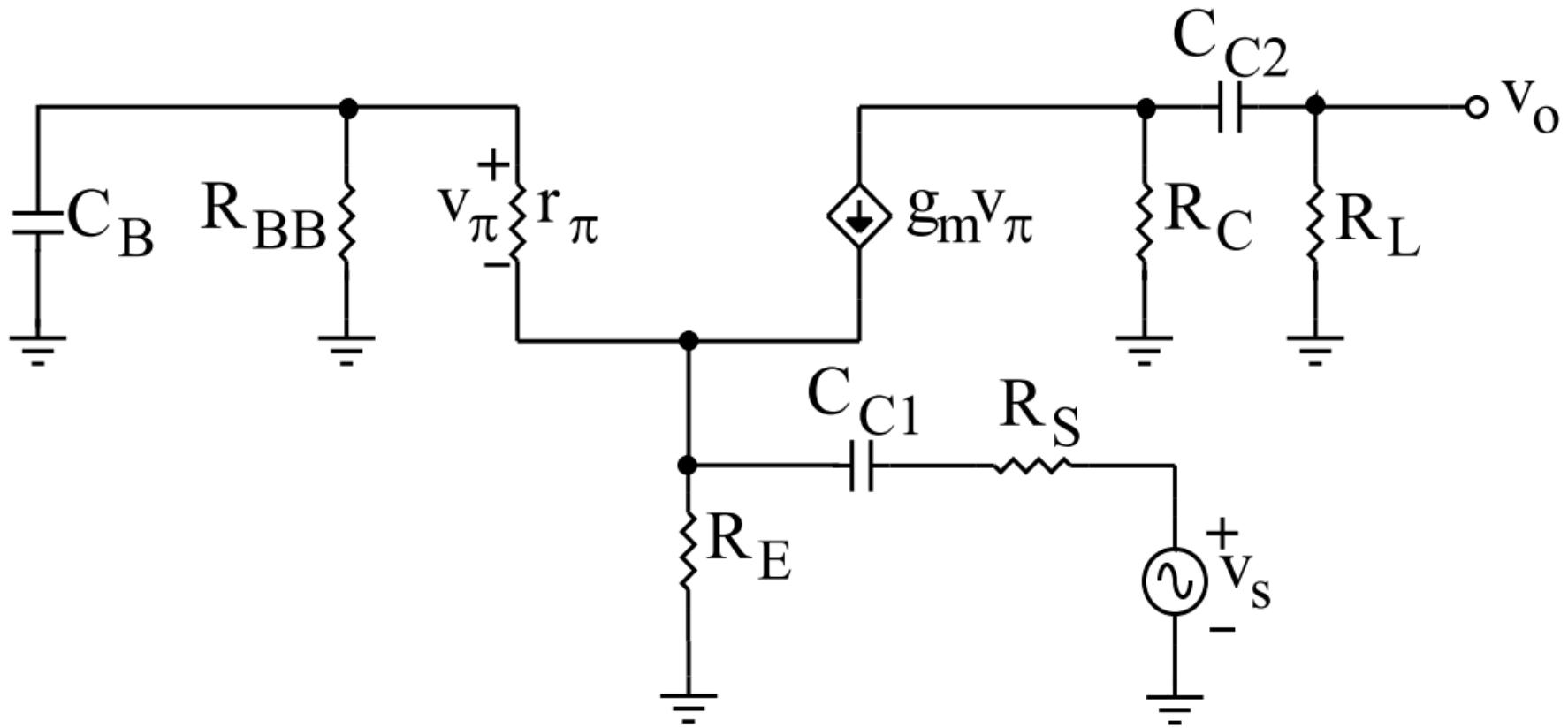
$$F(s) = \underbrace{F_L(s)}_{LF\ part} \underbrace{A_M}_{Midband} \underbrace{F_H(s)}_{HF\ part}$$



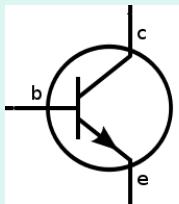


Low-frequency small-signal model

- The HF capacitors are open-circuited

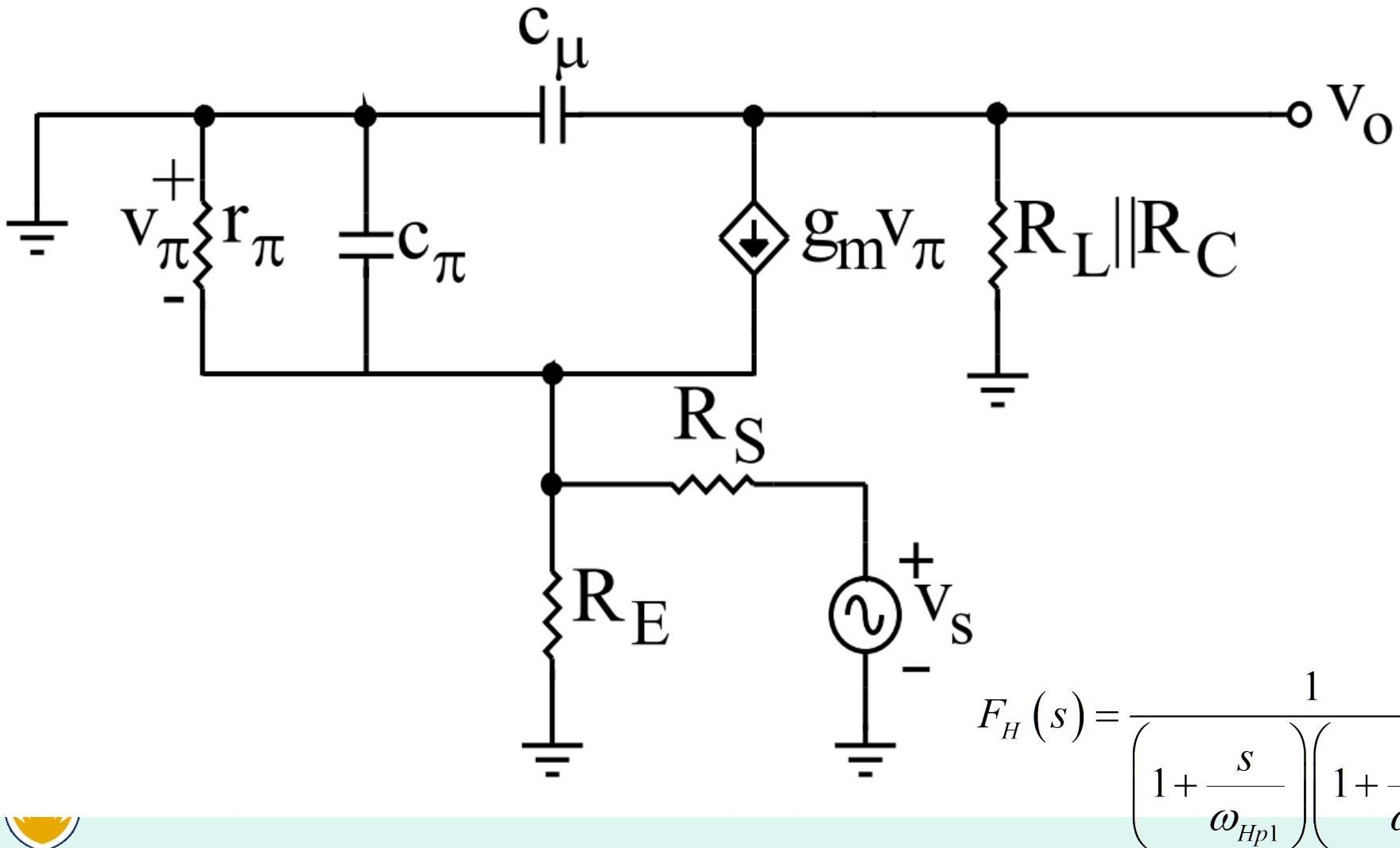


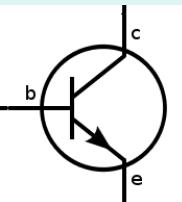
$$F_L(s) = \frac{(s + \omega_{Lz1})(s + \omega_{Lz2})(s + \omega_{Lz3})}{(s + \omega_{Lp1})(s + \omega_{Lp2})(s + \omega_{Lp3})}$$



High-frequency small signal model

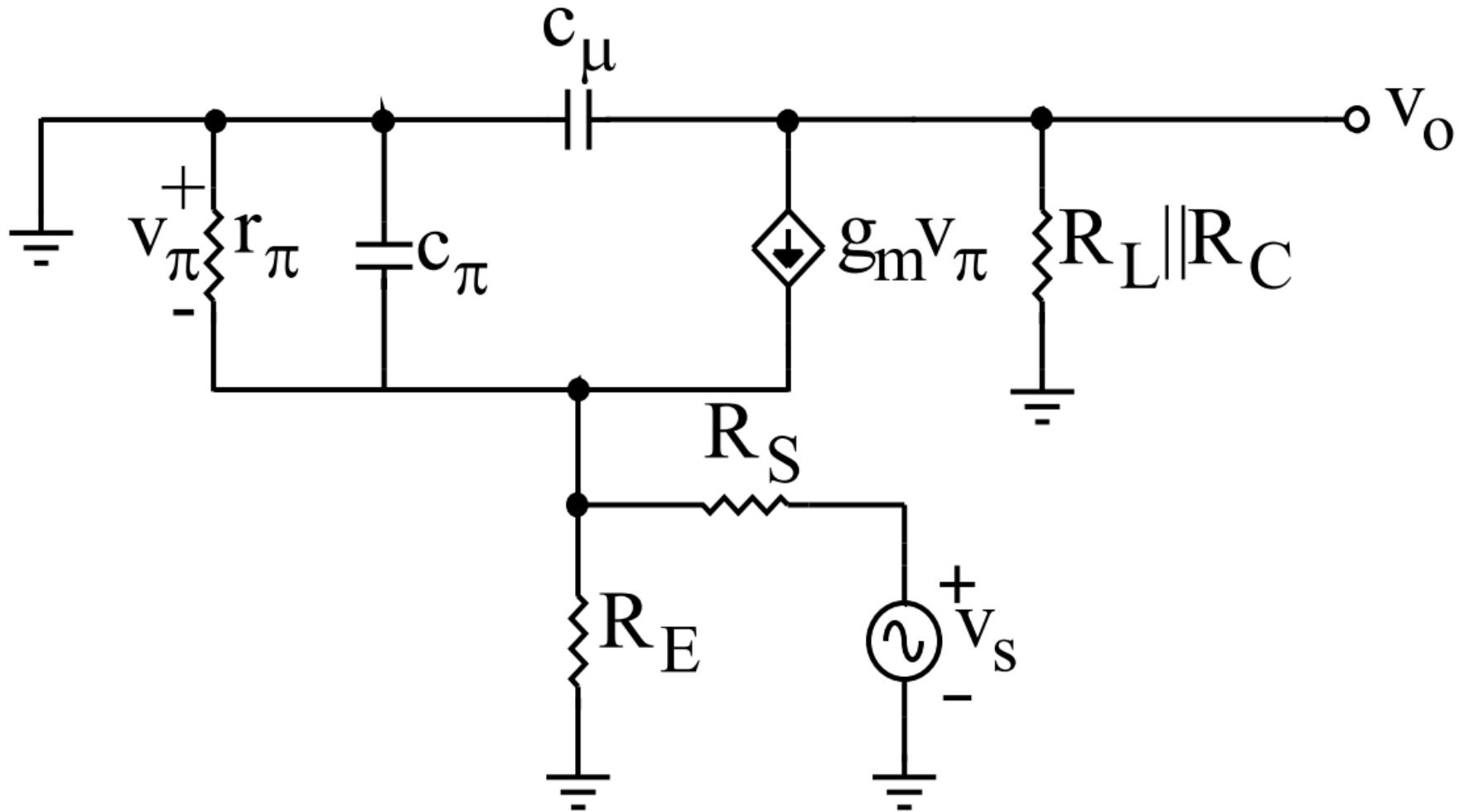
- The LF capacitors are short-circuited

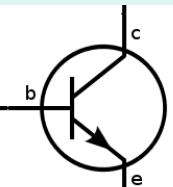




High-frequency small signal model

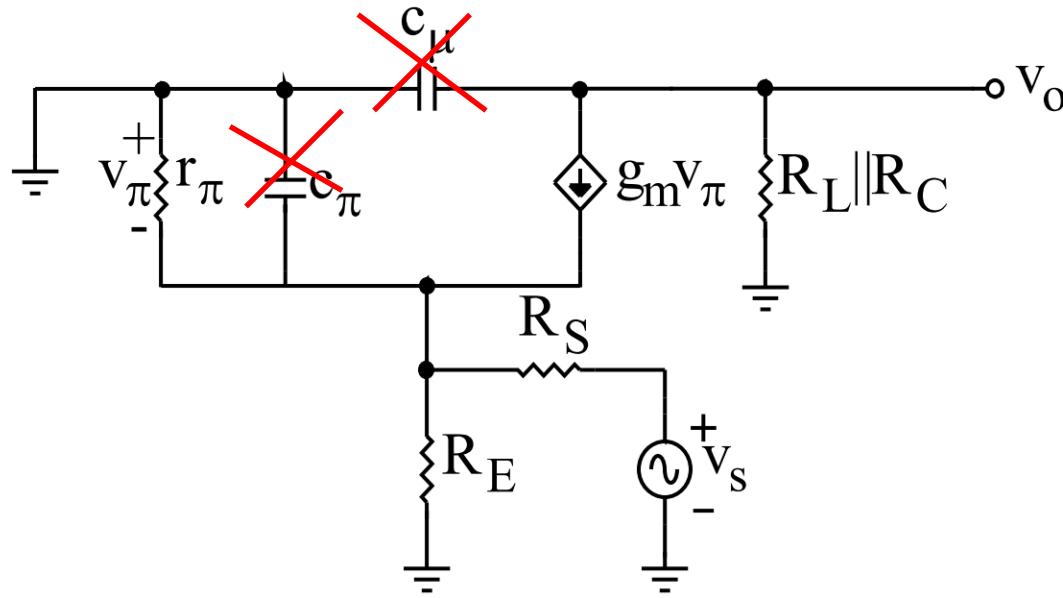
- The LF capacitors are short-circuited





Mid-band gain

- The junction capacitances C_μ, C_π treated as OC
- REM: r_π is reduced by $(\beta+1)$ times when looking from E



$$v_\pi = -\frac{\frac{r_\pi}{1+\beta} \| R_E}{R_S + \frac{r_\pi}{1+\beta} \| R_E} v_s \approx -\frac{\frac{r_\pi}{1+\beta}}{R_S + \frac{r_\pi}{1+\beta}} v_s$$

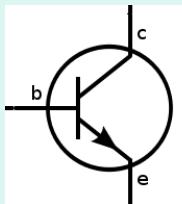
$$R_{E,eq} \Big|_{CB} = R_E \parallel \frac{r_\pi}{\beta + 1}$$

$$A_M \Big|_{CE} = -g_m R_C \parallel R_L \frac{R_{BB} \parallel r_\pi}{R_{BB} \parallel r_\pi + R_S}$$

$$R_{B,eq} \Big|_{CE} = R_{BB} \parallel (r_\pi + (\beta + 1) R_E)$$

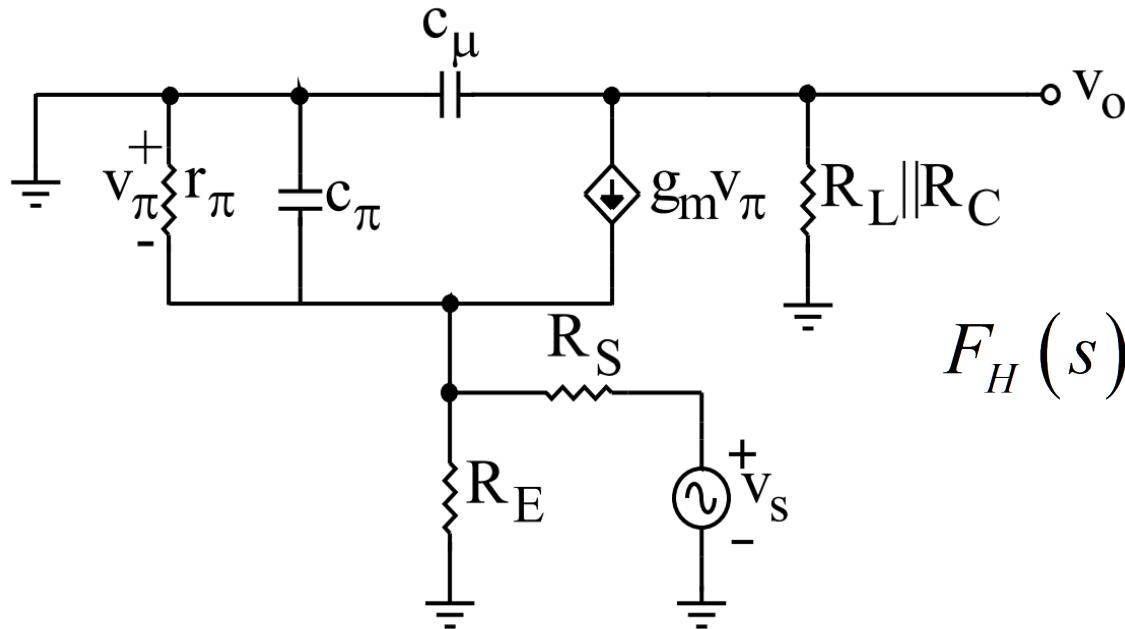
$$A_M \Big|_{CB} = g_m R_C \parallel R_L \frac{\frac{r_\pi}{\beta + 1} \parallel R_E}{R_S + \frac{r_\pi}{\beta + 1} \parallel R_E}$$



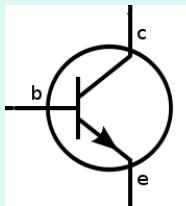


High-frequency behavior - $F_H(s)$

- No Miller multiplication of C_μ in the input circuit
- poles given by C_μ , C_π

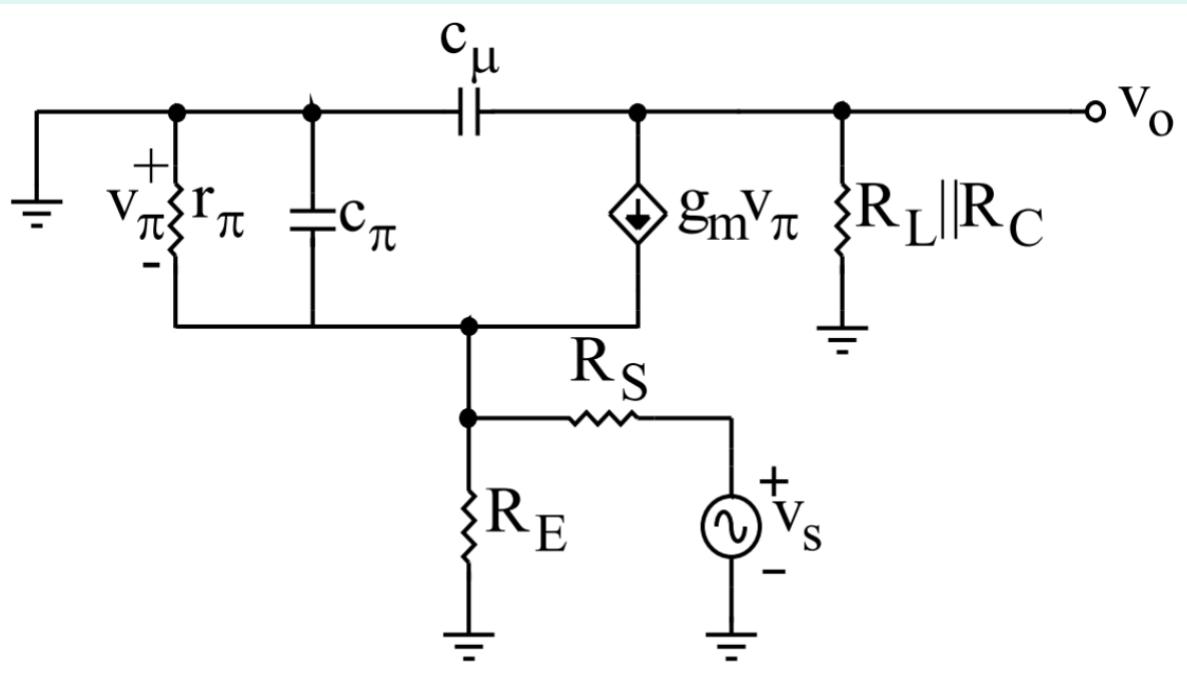


$$F_H(s) = \frac{1}{\left(1 + \frac{s}{\omega_{Hp1}}\right)\left(1 + \frac{s}{\omega_{Hp2}}\right)}$$



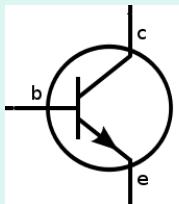
C_μ - component

- C_π is OC



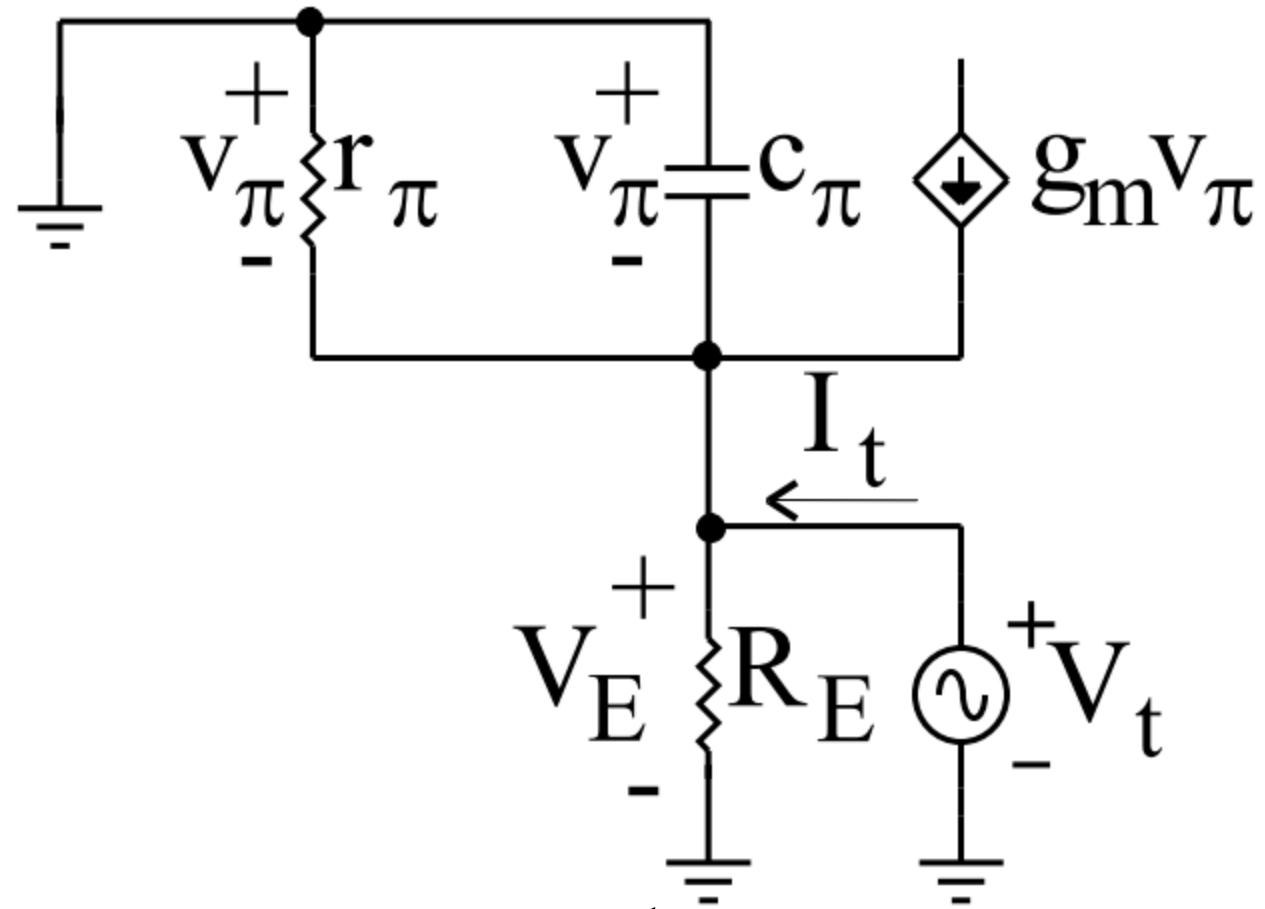
$$R_{C_\mu}^{OC} = R_L \parallel R_C \Rightarrow \omega_{Hpl}^{OC} = \frac{1}{(R_L \parallel R_C) C_\mu}$$



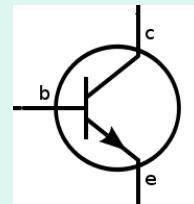


C_π component

- C_μ is OC



$$R_{C_\pi}^{OC} = R_S \parallel R_E \parallel \frac{r_\pi}{\beta + 1} \Rightarrow \omega_{H_{p2}}^{OC} = \frac{1}{\left(R_S \parallel R_E \parallel \frac{r_\pi}{\beta + 1} \right) C_\pi}$$



$$F_H(s)$$

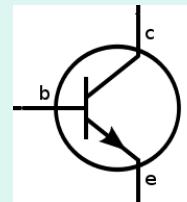
- Apply the OC method

$$\frac{1}{\omega_{H3dB}} = \frac{1}{\omega_{Hp1}^{OC}} + \frac{1}{\omega_{Hp2}^{OC}} = (R_L \parallel R_C) C_\mu + \left(R_S \parallel R_E \parallel \frac{r_\pi}{\beta + 1} \right) C_\pi \approx (R_L \parallel R_C) C_\mu$$

For the second pole (sub-dominant): if the lowest pole corresponds to C_μ , then we estimate the second pole with C_μ short-circuited \rightarrow it does not change the second pole position

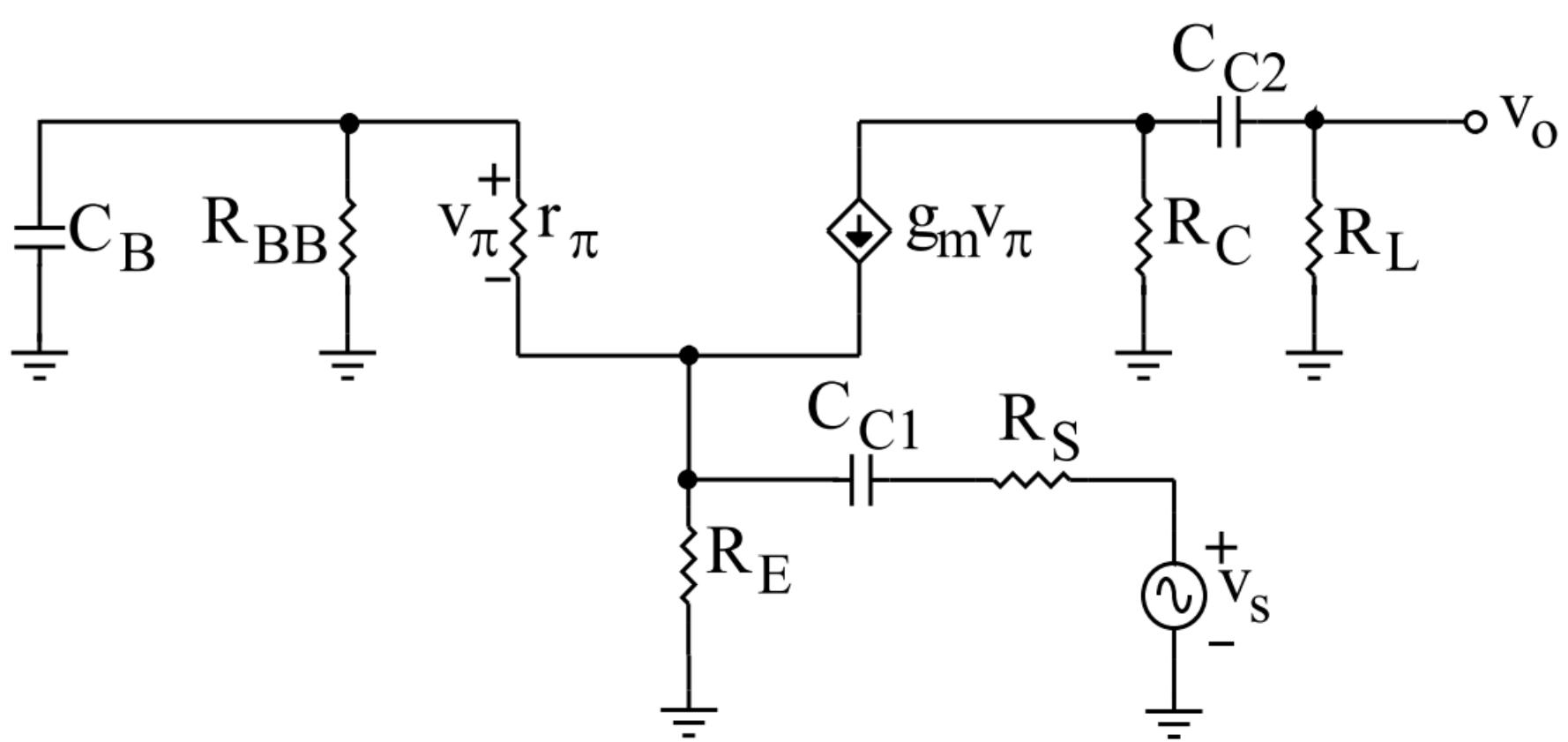
$$F_H(s) = \frac{1}{\left(1 + s(R_L \parallel R_C) C_\mu\right) \left(1 + s\left(R_S \parallel R_E \parallel \frac{r_\pi}{\beta + 1}\right) C_\pi\right)}$$



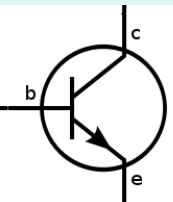


CB - LF behavior $F_L(s)$

- We get back to the LF circuit - 3poles + 3 zeros

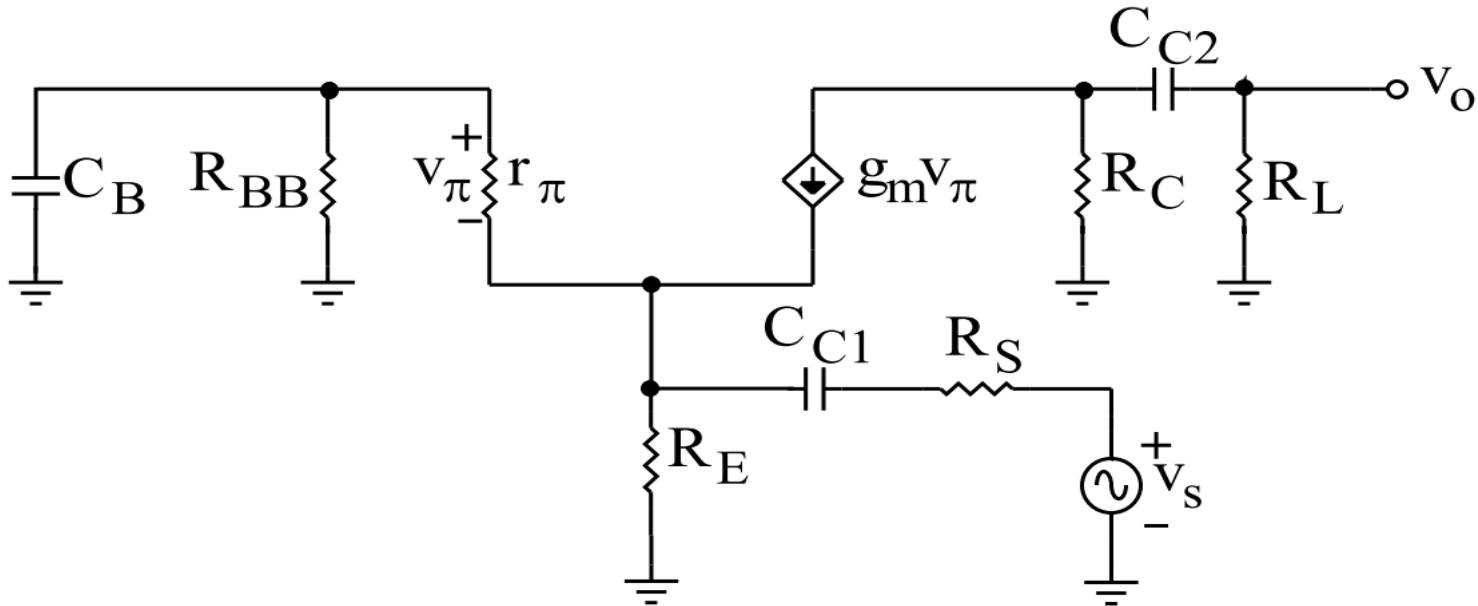


$$F_L(s) = \frac{(s + \omega_{Lz1})(s + \omega_{Lz2})(s + \omega_{Lz3})}{(s + \omega_{Lp1})(s + \omega_{Lp2})(s + \omega_{Lp3})}$$



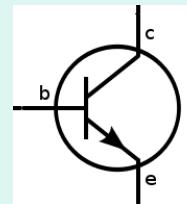
FL(s) - zeros

- Zeros: C_{C1}, C_{C2} introduce zeros at $\omega=0$
- For CB - zero located when $v_\pi=0$ (or $i_b=0$)



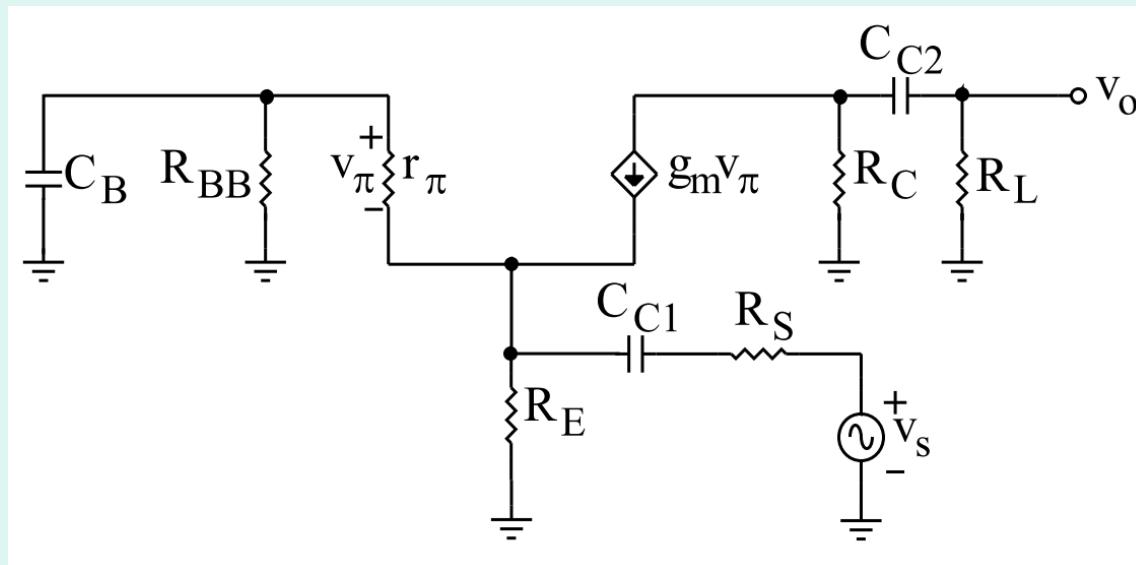
$$Y_B = s_z C_B + \frac{1}{R_{BB}} = 0 \Rightarrow s_z = -\frac{1}{R_{BB} C_B} \Rightarrow \omega_{Lz3} = \frac{1}{R_{BB} C_B}$$





$F_L(s)$ - poles

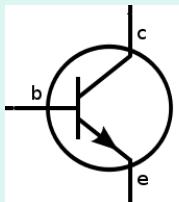
- The pole associated with the output stage (decoupled from input) is straight forward



$$R_{C_{C2}} = R_C + R_L \Rightarrow \tau_{C_{C2}} = (R_C + R_L) C_{C2}$$

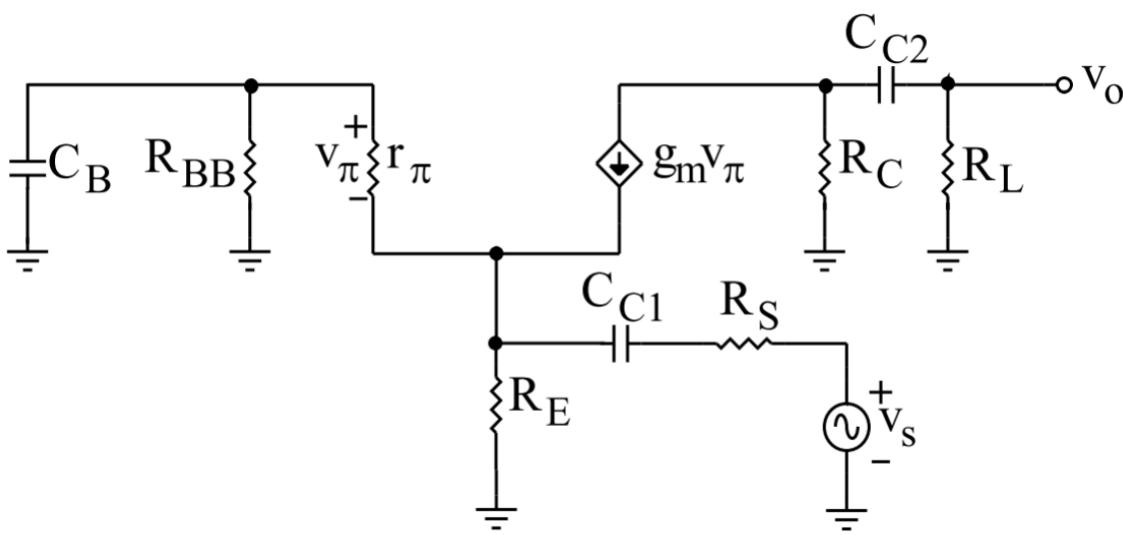
$$\omega_{Lp1} = \frac{1}{(R_C + R_L) C_{C2}}$$





$F_L(s)$ - remaining 2 poles

- We use the SC time constant method (assuming the poles are well distanced)



When C_{C1} is SC $\Rightarrow R_E \parallel R_S$ reflected into the B

$$R_{C_B}^{SC} = R_{BB} \parallel (r_\pi + (\beta + 1)R_E \parallel R_S) \Rightarrow \tau_{C_B}^{SC} = (R_{BB} \parallel (r_\pi + (\beta + 1)R_E \parallel R_S)) C_B$$



