

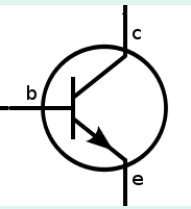


# ELEC 301 - CC amplifier (2)

L16 - Oct 14

Instructor: Edmond Cretu





## Last time

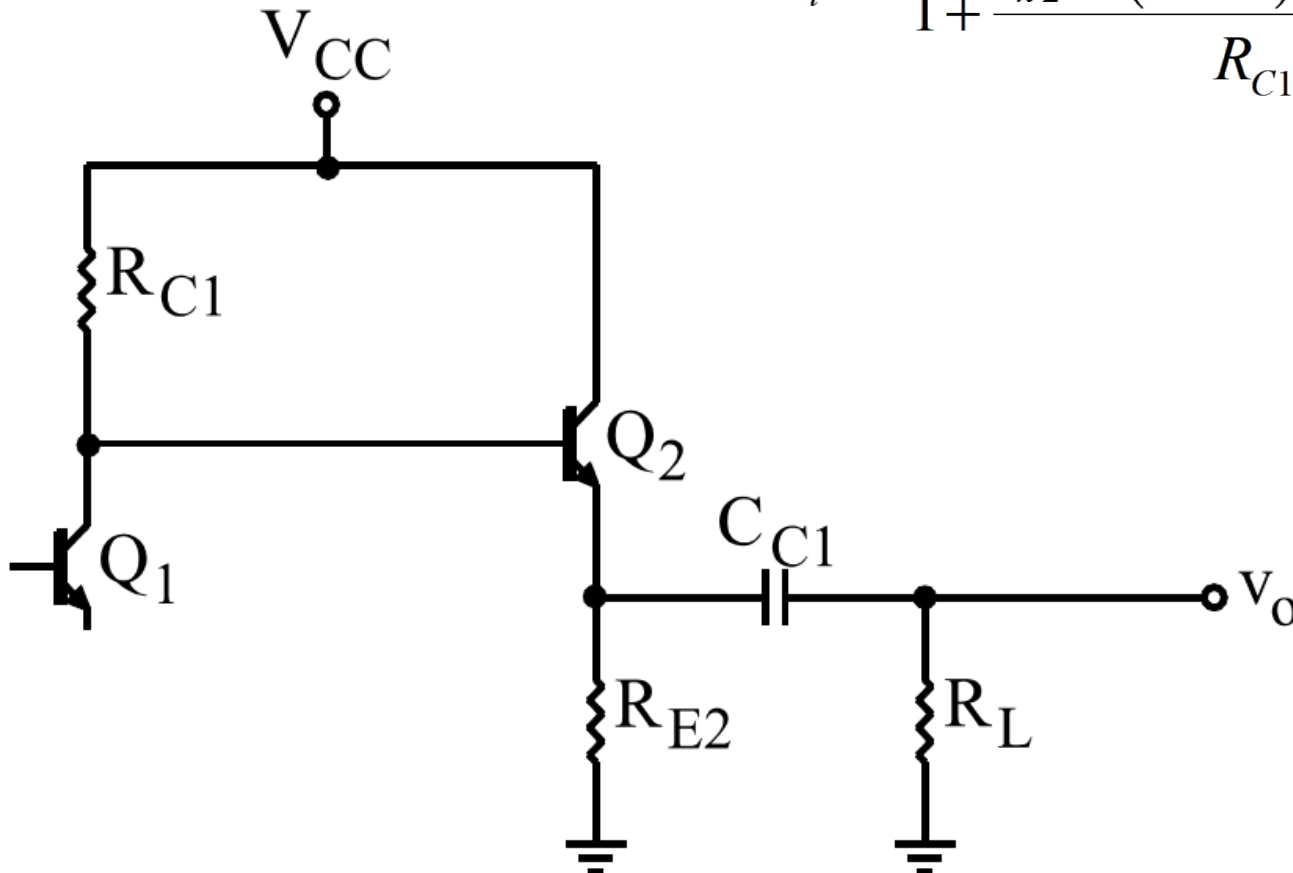
- Ideal amplifier diports: voltage amplifier, current amplifier, transimpedance amplifier, transadmittance amplifier
- CB amplifier
- CC amplifier: high input impedance, low output impedance, power gain, DC coupled at input, wide BW

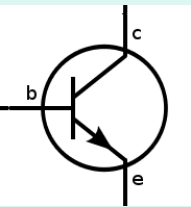


# CC amplifier

- current gain, almost unity voltage gain

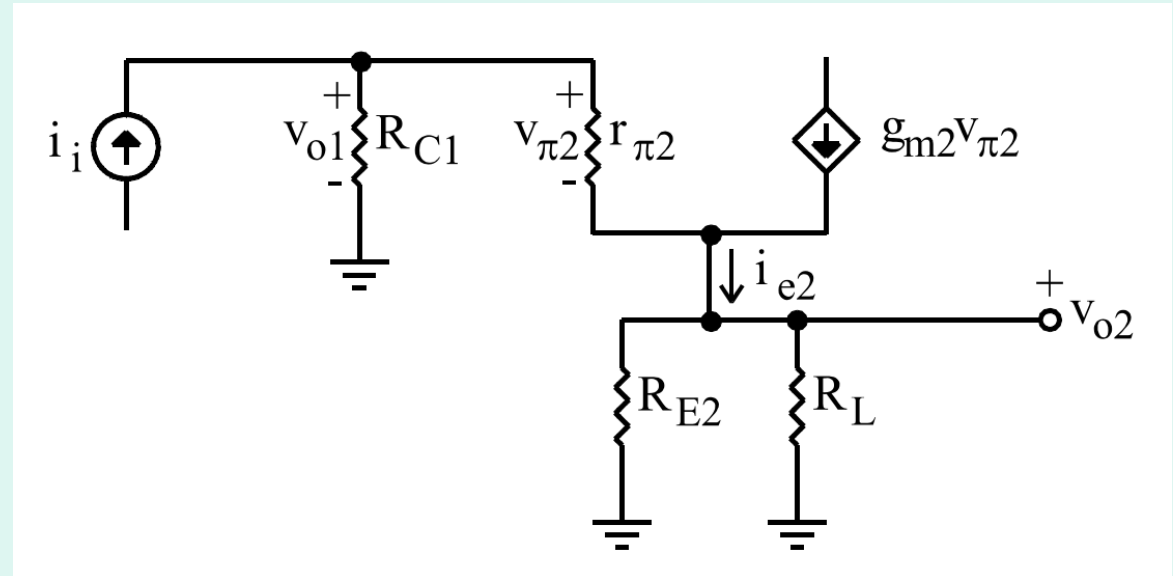
$$A_i = \frac{i_{e2}}{i_i} = \frac{\beta + 1}{1 + \frac{r_{\pi 2} + (\beta + 1) R_{E2} \parallel R_L}{R_{C1}}} \approx \frac{R_{C1}}{R_{E2} \parallel R_L}$$





# CC amplifier - voltage gain

- $A_{v2} = v_{o2}/v_{o1} \sim 1 \Rightarrow$  the power gain is given by the current gain



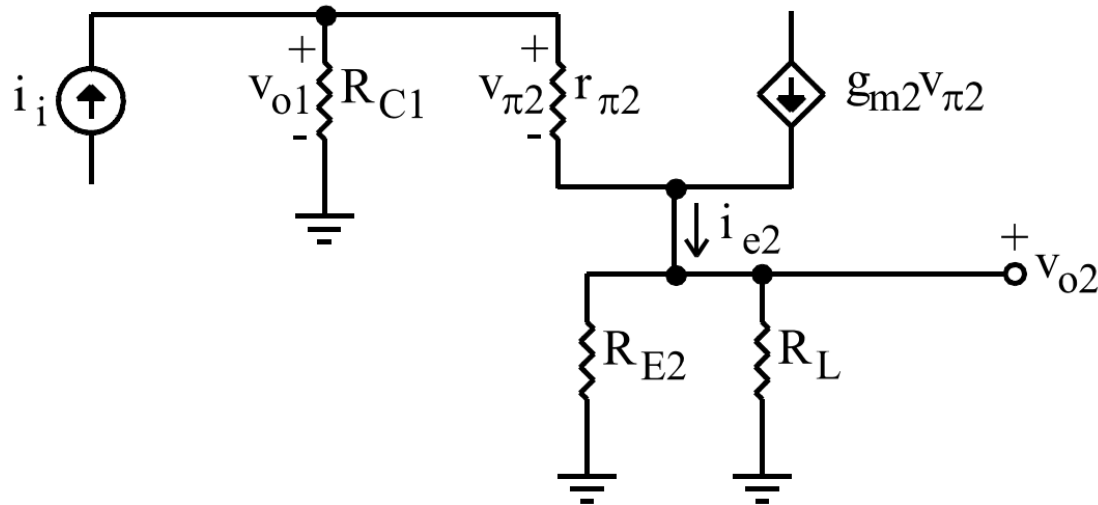
$$v_{o2} = (R_{E2} \parallel R_L) i_{e2} = (R_{E2} \parallel R_L) \frac{(\beta + 1) v_{o1}}{r_{\pi 2} + (\beta + 1) R_{E2} \parallel R_L}$$

$$A_{v2} = \frac{v_{o2}}{v_{o1}} = \frac{(\beta + 1)(R_{E2} \parallel R_L)}{r_{\pi 2} + (\beta + 1) R_{E2} \parallel R_L} \leq 1$$



## CC amplifier - output impedance at midband

- Remove  $R_L$ , look from  $v_{o2}$  - low output impedance

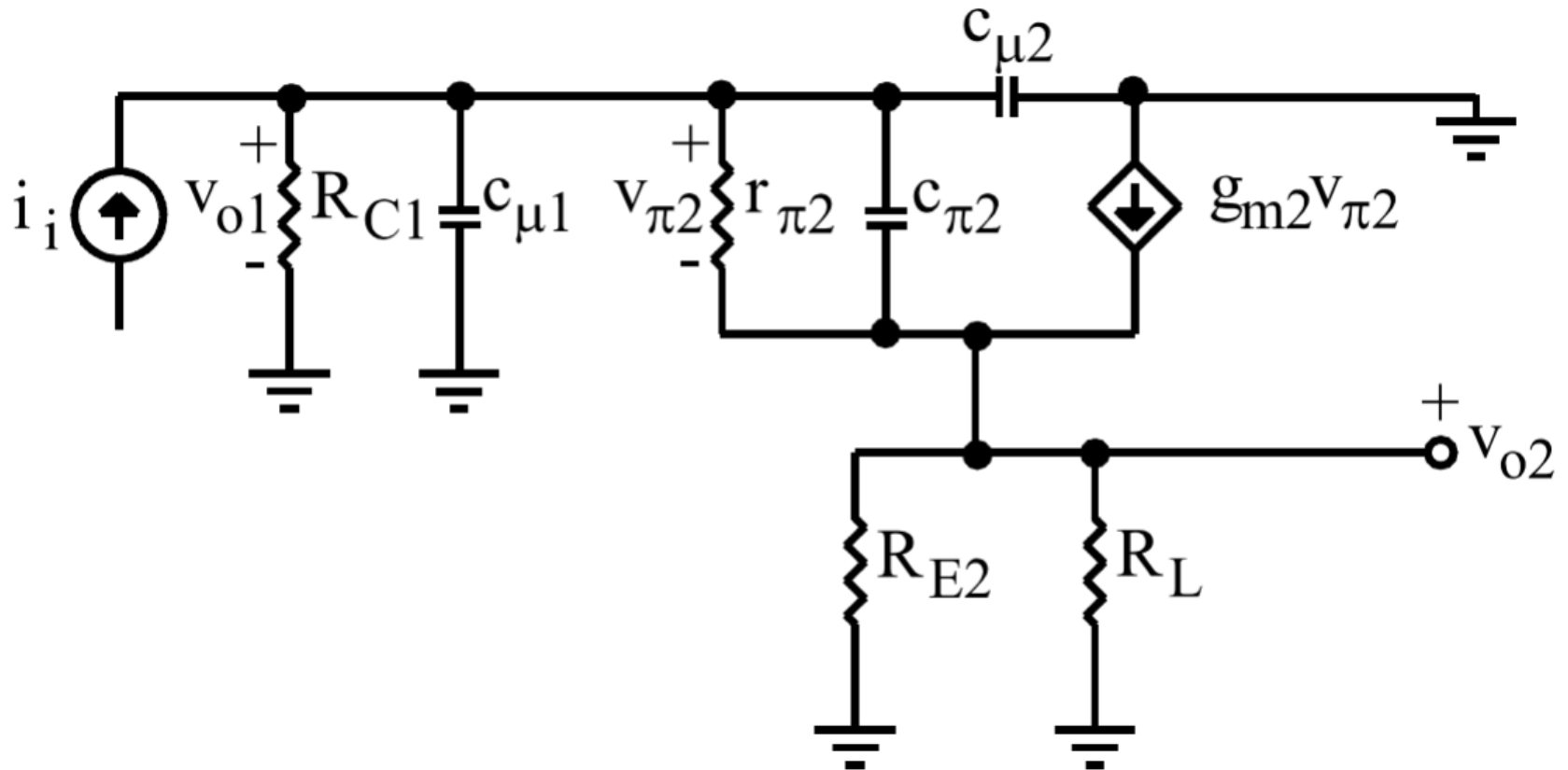


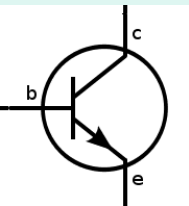
$$R_{o2} = R_{E2} \parallel \frac{r_{\pi 2} + R_{C1}}{\beta_2 + 1} \approx \frac{r_{\pi 2} + R_{C1}}{\beta_2 + 1}$$



## $F_H(s)$ - HF response

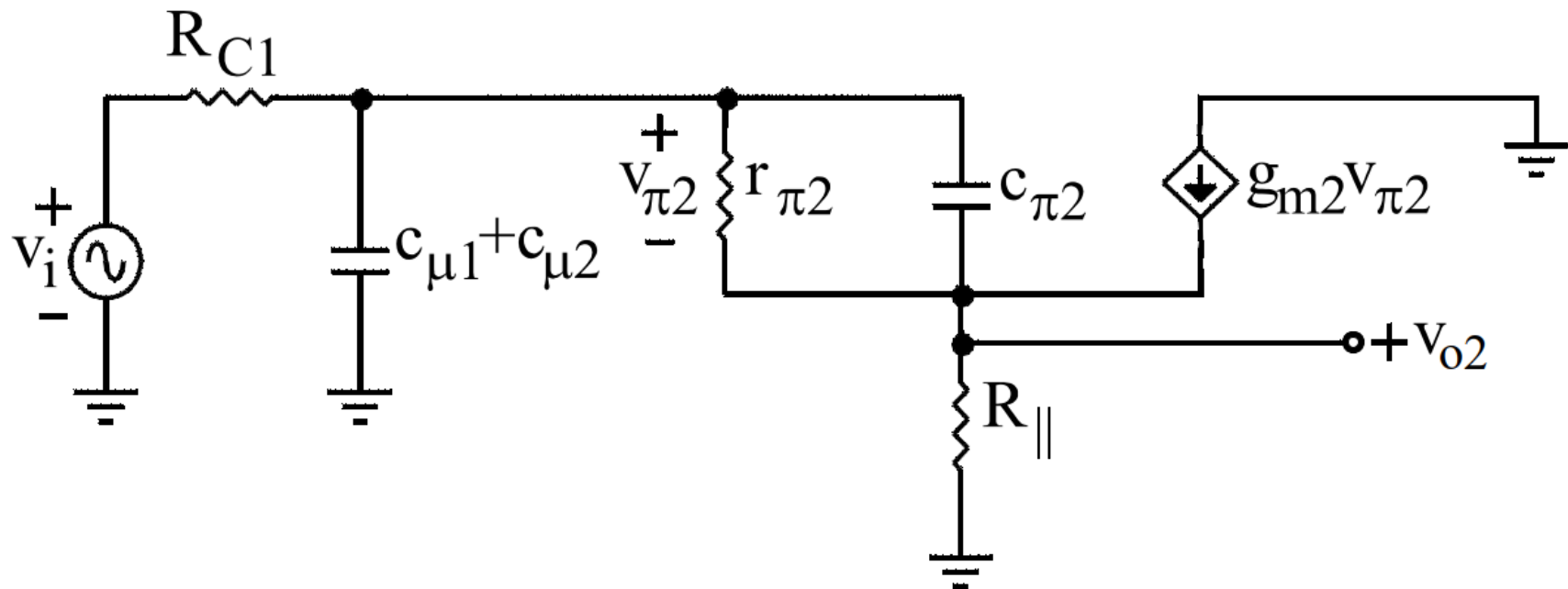
- HF small-signal circuit

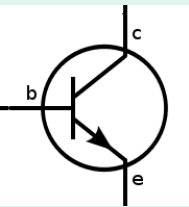




# HF response - redrawn circuit

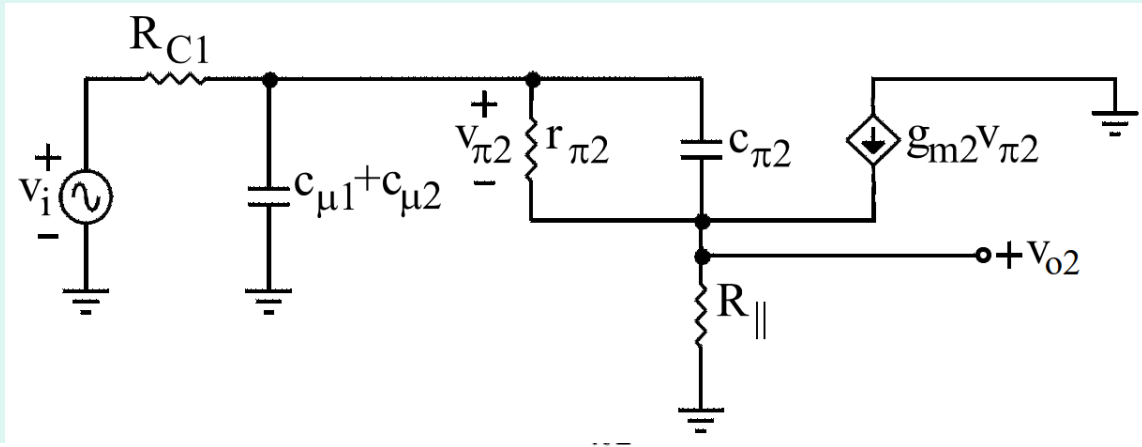
- $R_{||} = R_{E2} || R_L$ ,  $v_i = R_{C1} i_i$





# $C_{\pi 2}$ OC and SC time constants

- For  $C_{\pi 2}$

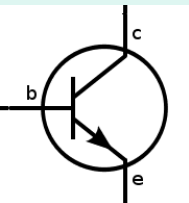


$$\tau_{c\pi 2}^{oc} = \left( c_{\pi 2} \times \frac{r_{\pi 2}}{R_{in2}} \right) \left( R_{C1} \parallel R_{in2} \right) \left( 1 + \frac{R_{||}}{R_{C1}} \right) \approx$$

$$\left( c_{\pi 2} \times \frac{r_{\pi 2}}{R_{in2}} \right) \left( R_{C1} \parallel R_{in2} \right)$$

$$\tau_{c\pi 2}^{sc} = c_{\pi 2} R_{||} \parallel \frac{r_{\pi 2}}{1 + \beta_2} \approx c_{\pi 2} \frac{r_{\pi 2}}{1 + \beta_2}$$





# CC HF - dominant high frequency

- Dominant pole  $\omega_{Hp1}$

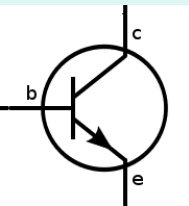
$$\frac{1}{\omega_{H3dB}} = \frac{1}{\omega_{C_\mu}^{OC}} + \frac{1}{\omega_{C_\pi}^{OC}} = \tau_\mu^{OC} + \tau_\pi^{OC} \quad \tau_\mu^{oc} = R_{C1} \parallel \underbrace{\left( r_{\pi2} + (\beta + 1) R_{\parallel} \right)}_{R_{in2}} (C_{\mu1} + C_{\mu2})$$

$$\omega_{Hp1} \approx \frac{1}{(c_{\mu1} + c_{\mu2}) R_{C1} \parallel R_{in2}}$$

$$\tau_{\pi2}^{oc} = \frac{r_{\pi2} R_{C1}}{r_{\pi2} + (\beta_2 + 1) R_{\parallel} + R_{C1}} C_{\pi2}$$

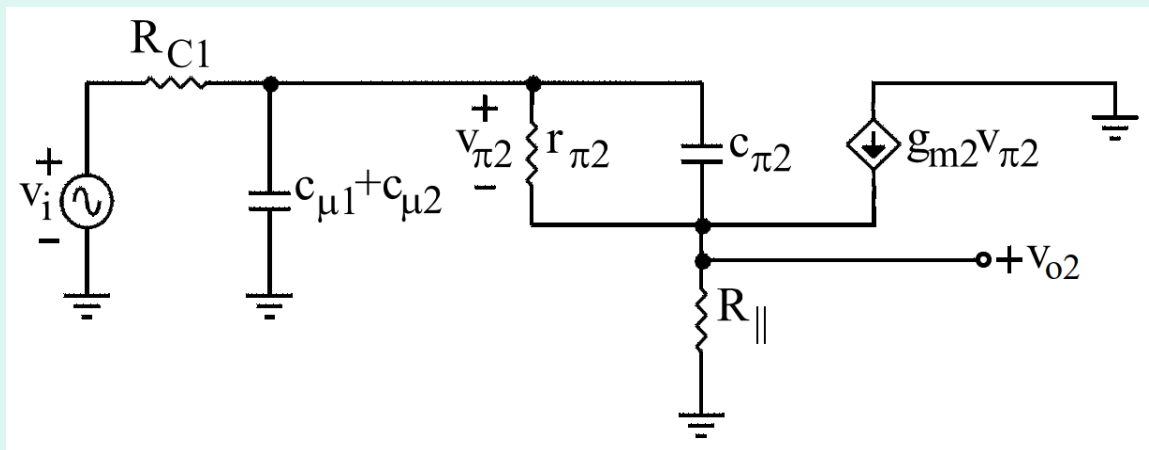
The sub-dominant pole  $\omega_{Hp2}$ :

$$\omega_{Hp2} \simeq \frac{1}{\tau_{\pi2}^{sc}} \approx \frac{\beta_2 + 1}{r_{\pi2} C_{\pi2}}$$



# CC - HF zero

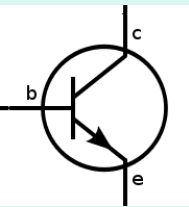
- This circuit also has a high frequency zero



$$v_{o2} = 0 \Leftrightarrow R_{\parallel} (y_{\pi 2} v_{\pi 2} + g_{m2} v_{\pi 2}) = 0 \quad \frac{1}{r_{\pi 2}} + s_{Hz} C_{\pi 2} + \underbrace{\frac{\beta_2}{r_{\pi 2}}}_{g_{m2}} = 0 \Rightarrow s_{Hz} = -\frac{\beta_2 + 1}{r_{\pi 2} C_{\pi 2}}$$

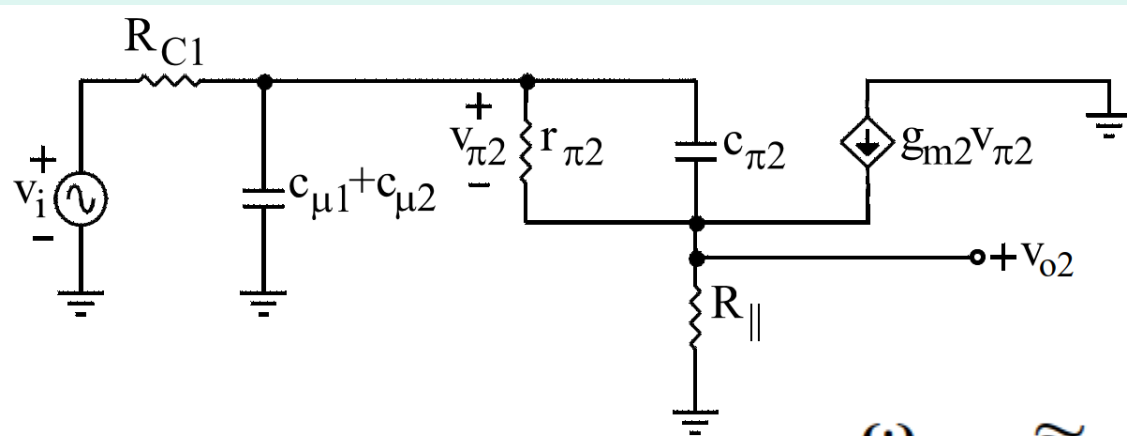
The HF zero and the sub-dominant HF pole are nearly coincident and cancel each other out - this is known as “**pole-zero cancellation**” (used sometimes in the control system to tailor the frequency response of a system)

$$\frac{\frac{s}{\omega_{Hz}} + 1}{\frac{s}{\omega_{Hp2}} + 1} \approx 1$$



# CC HF response

- Very similar to a first order LP filter



$$F_H(s) \approx \frac{\omega_{Hp}}{s + \omega_{Hp}}$$

$$\omega_{Hp} \approx \frac{1}{(c_{\mu 1} + c_{\mu 2}) R_{C1} \parallel R_{in2}}$$

When similar transistors are used so that  $C_{\mu 1} \approx C_{\mu 2}$

$$\omega_{Hp} \approx \frac{1}{2 c_{\mu 1} R_{C1} \parallel R_{in2}}$$

